

January 2012 International GCSE Mathematics (4MA0) Paper 3H Mark Scheme

Question	Working	Answer	Mark	Notes
1. (a)	$7/32 \times 100$ oe	21.9	2	M1 A1 (21.875) accept awrt to 21.9
(b)	$4/100 \times 32$ (=1.28) or $4/100 \times 3200000$ (=1280000) or $32 + "1.28"$ or $3200000 + "1280000"$	33	3	M1 M1 M1 A1 M2 for 32×1.04 oe or 3200000×1.04 oe (dep) (33.28) accept 33.3, 33000000, 33300000, 33280000
				Total 5 marks

2.	$2/5 \times 30$	12	2	M1 A1 12 out of 30 = M1A1 12/30 = M1A0
				Total 2 marks

3.	$\pi \times 7.5^2 \times 26$	4590	3	M2 A1 M1 for $\pi \times 15^2 \times 26$ or 18369 \rightarrow 18386 inc (4594.579....) accept answers 4592 \rightarrow 4597 inc
				Total 3 marks

4.	Arcs of length 6cm from A <u>and</u> B			M1
	Arc of length 10 cm from A <u>or</u> B			M1
	Arc of length 6 cm from correct top vertex			M1
	Correct rhombus within overlay tolerance		4	A1 sc B1 for correct rhombus with no construction lines.
				Total 4 marks

5. (a)		$a(5 - 3a)$	2	B2 B1 for factors which when expanded & simplified give 2 terms for which one is correct.
(b) (i)		$8 - 6w$	1	B1
(ii)		$y^2 + 10y^2$	2	B2 B1 for y^3 or $10y^2$
(c)	$7.168 / 0.64$	11.2	2	B2 B1 for 7.168 or 0.64
				Total 7 marks

6. (a) (i)	Does not study Maths No student studies (both) German and Maths Students who study German do not study Maths etc	1	B1	Accept general answers (e.g. no student belongs in both sets).
(ii)	(Preety) does not study French (Preety) is not a member of (set) F	1	B1	Accept she /he in place of Preety or omission of name. Penalise extra incorrect statements (e.g. Preety studies Maths and German but not French)
(b)	1,2,3,4	2	B2	B1 for any 3 correct with no repetitions or additions.
				Total 4 marks

7. (a)	9 to 11	1	B1	
(b) (i)	$(1 \times 3) + (4 \times 6) + (7 \times 10) + (10 \times 15) + (13 \times 5) + (16 \times 1)$ (=328) "328" \div ("3+6+10+15+5+1")		M2	All products, $t \times f$ using $\frac{1}{2}$ way points correctly, and intention to add. Award M1 if all products, $t \times f$ using their $\frac{1}{2}$ way points consistently, from 6 to 8 interval onwards and intention to add.
(ii)	Mid-points used as actual data is unknown	4	M1 A1	(dep on one at least M1) Accept 8 with working. 8 without working = M0A0
		1	B1	Mention of mid-points or exact (actual) data is unknown.
				Total 6 marks

8. (a)	$x/60$ oe	1	B1	Must be a fraction or 0.016 rec x
(b) (i)	$2("x/60") = (x+20)/80$ $16(0) x = 6(0)(x + 20)$ or $80 x = 30(x + 20)$ or $2x/3 = (x + 20)/4$	3	M2 (must be an equation) A1 dep	M1 for either $2("x/60")$ or $(x+20)/80$ Correct removal of denominators.
(ii)	$8x = 3x + 60$ or $5x = 60$ or $60 \div 5$	2	M1 A1	Correct removal of denominators. Simplifying denominators. Dependent on M1. Can be marked if seen in b(i)
				Total 6 marks

9. (a)	Use of sine or $\frac{\sin x}{3.4} = \frac{\sin 90}{5.8}$			M1	Sine must be selected for use.
	$\sin "x" = 3.4 / 5.8 (=0.586..)$	35.9	3	M1 A1 (35.888...)	Use isw on awrt 35.9
(b) (i)		5.85	1	B1	accept 5.849 rec
	(ii)	5.75	1	B1	
Total 5 marks					

10.	6/100 x 7500 (=450) {1st Year} or 1.06 x 7500 (=7950)			M1	M2 for $1.06^3 \times 7500 (=8932.62)$
	"450" + "477" + "505.62"	1432.62	3	M1 A1	Calculating 6% of previous capital for another 2 years. M1A0 for 1350 or 8850
Total 3 marks					

11.	$3y + 6x - 3 = x + 5y$			M1	Multiplying out brackets.
	$5x - 3 = 2y$ oe	$(5x - 3)/2$	3	M1 dep A1 oe	Correctly collecting like terms, (3 terms needed here).
Total 3 marks					

12. (a)	6/9 x 12 oe	8	2	M1 e.g 12 ÷ 1.5 A1	
	9/6 (or 12/"8") x 5	7.5	2	M1 A1 cao	
(c)	$1.5^2 \times 32 (=72)$ oe			M1	M1 for 1.5^2 or $(2/3)^2$
	"72" - 32	40	3	M1 dep A1	
Total 7 marks					

13. (a) (i)		Angles in same segment (are equal)	2	B1	Accept "from same chord", "on same arc".
	(ii)			B1	
(b) (i)		41°		B1	
	(ii)	75°		B1	
		Angle at centre/middle is not 2 x angle at circumference / edge / perimeter / arc or Angle PQT ≠ QPT or PRS ≠ RSQ (oe) or 34 ≠ 41	2	B1	Accept $75 \neq 2 \times 41$ or $75 \neq 2 \times 34$ or using idea of isosceles triangles but must mention angles.
	Total 4 marks				

14. (a)	$y = 36 - x$			M2 A1	M1 for $x + y = 36$ oe or $2y = 72 - 2x$ Must see x times $(36 - x)$ dep on M2	Total 8 marks
(b)			$(\text{Area} =) x (36 - x)$	3		
(c)	$36 - 2x^2 = 0$ $x = 18$		$(dA/dx) = 36 - 2x$ (Area =) 324	2 3	B1 B1 M1 A1ft A1ft	

15. (a)	$F = "k"/d^2$ $12 = k/2^2$ $k = 48$			M1 M1	k= letter not number.	Total 6 marks
(b)	$(F =) "48"/5^2$		$F = 48/d^2$	3	Award 3 marks for $F = "k"/d^2$ and $k = 48$ stated anywhere, unless contradicted by later work.	
(c)	$3 = "48"/d^2$ $d^2 = "48"/3$		1.92 oe	1	B1 ft $k \neq 1$ accept 48/25 as an answer.	
				2	Rearrangement to make d^2 or d the subject ignore \pm	

16. (a)	10×3 or 15×2 or $12 \times 7.5/3$			M1	or any correct fd in correct position and no errors, or 1 sq = 2 (runners) indicated.	Total 6 marks
(b)	Missing blocks = 6cm, 10cm, 2cm		30	2	3 correct blocks B1 1 or 2 correct blocks	
(c)	$0.6 \times 20 + 0.8 \times "30"$ or $3 \times "4" + 8 \times "3"$ or 450×0.08			M1	(partitioning blocks) (time x fd's) {must see clear evidence that fd values used}. 450 small squares.	
			36	2	A1 cao	

17.	$x = 0.1777 \dots$ and $10x = 1.777 \dots$ $9x = 1.6$			M1 A1	See at least 3 sevens or recurring symbol. Condone omission of x. Accept $10x = 1.777 \dots$ and $100x = 17.77 \dots$ Must be integers in numerator and denominator but not 8 & 45 N.B for $0.1777 = 1/10 + 0.0777 \dots$ (0.777 needs to be shown to be 7/90 to gain first M1)	Total 2 marks
			16/90 oe			

18.	AOC = 70° “70”/360 x π x 9 ² (=49.48..) 0.5 x 9 ² x sin “70” = (38.057..) 49.48.. or 38.057... “49.48..” – “38.057..”				B1 M1ft M1ft A1 M1 A1 Could be marked on diagram. Area of sector. Area of triangle. Follow through angles must be the same. Either area correct to 3 sf dep on both previous M1's (11.42253...) awrt 11.4	Total 6 marks
			11.4	6		

19.	$\frac{(\sqrt{3} + 3\sqrt{3})/\sqrt{2}}{4\sqrt{3}/\sqrt{2}}$ 2√6 or (√48 /√2)				M1 M1 A1cao Must see √27 reduce to 3√3 dep on 1st M1 dep on M2 Accept √24 if M2 awarded.	alternative $\frac{\sqrt{6} + \sqrt{54}}{2}$ (or better)
			24	3		Total 3 marks
20.	$\frac{4(2-x)+3x}{x(2-x)}$ oe $\frac{8-4x+3x}{x(2-x)}$				M1 M1 A1 Accept Single fraction needed as final answer.	
			$\frac{8-x}{x(2-x)}$	3		Total 3 marks

21. (a)	$0.5x[(x + 5) + (x + 8)] = 42$ (trapezium formula) or $x(x + 5) + 0.5x(x + 8) = 42$ (partitioning) $x(2x + 13) = 84$ or $x^2 + 5x + 1.5x = 42$		2	M1 dep on 1 st M1 then needs to develop on to quadratic given. M1
(b)	$(2x + 21)(x - 4) (= 0)$ oe $x = 4$ (P=) "4" + "9" + "12" + $\sqrt{(3^2 + 4^2)}$	30	5	B2 B1 for either factor correct or $(2x \pm 21)(x \pm 4)$ or M1 for $x = \frac{-13 \pm \sqrt{13^2 - 4 \times 2 \times -84}}{4}$ (condone 1 sign error) then M1 for $x = \frac{-13 \pm \sqrt{169 + 672}}{4}$ A1 dep on M1 or B2 M1 i.e. $x + (x + 5) + (x + 8) + \sqrt{(3^2 + x^2)}$ in numeric form. A1cao (Last two marks independent) N.B. Working for solving quadratic could be seen in (a) if not contradicted in (b).
				Total 7 marks